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 $0 \in H$

tomamos $H = P_m(x)$, con $m < n$ y $P_m(x) = 0$.

\Rightarrow tomamos $P_m(x) = a_0 + a_1x + a_2x^2 + a_3x^3 + \dots + a_{n-1}x^{n-1}$

entonces $0 \in H$ dado que $0 = 0$.

$u, v \in H \Rightarrow u + v \in H$

tomamos $u = P_{n-1}(x)^{-1}$

Sea: $u = P_{n-1}(x)^{-1} = a_0 + a_1x + a_2x^2 + a_3x^3 + \dots + a_{n-1}x^{n-1}$

y $v = P_{n-1}(x)^{-1} = b_0 + b_1x + b_2x^2 + b_3x^3 + \dots + b_{n-1}x^{n-1}$

entonces tenemos

$v = a_0 + b_0 + (a_1 + b_1)x + (a_2 + b_2)x^2 + (a_3 + b_3)x^3 + \dots + (a_{n-1} + b_{n-1})x^{n-1}$
entonces $u + v = P_{n-1}(x)^{-1} + P_{n-1}(x)^{-1} \in H$

$u \in H$ y α , escalar $\Rightarrow \alpha u \in H$

Sea $u = P_{n-1}(x)$

$\alpha \cdot (a_0 + a_1x + a_2x^2 + a_3x^3 + \dots + a_{n-1}x^{n-1}) = (\alpha a_0 + (\alpha a_1)x$

$(\alpha a_2)x^2 + (\alpha a_3)x^3 + (\alpha a_4)x^4 + \dots + (\alpha a_{n-1})x^{n-1}$

$\therefore \alpha u = \alpha P_{n-1}(x) \in H$, con $H \in V$

es subespacio de V .

$\therefore H$ es subespacio vectorial